Exam 2

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**Directions:** Be sure to include in-line citations, including page numbers if appropriate, every time you use a text or notes or technology.

Only write on one side of each page.

## The Problems

- 1. Do any two (2) of the following.
  - (a) Using any result up to and including Proposition 3.4, prove **Pasch's Theorem.** If A, B, C are distinct non collinear points and l is any line intersecting segment AB in a point between A and B, then l also intersects either segment AC or segment BC. If C does not lie on l, then l does not intersect both AC and BC.
  - (b) Using any previous results, prove the following portion of Proposition 3.8. If D is in the interior of angle  $\triangleleft CAB$ ; then:
    - i. no point on the opposite ray to ray  $\overrightarrow{AD}$  is in the interior of angle  $\triangleleft CAB$ .
  - (c) Using any previous results, prove the **Crossbar Theorem**. If ray  $\overrightarrow{AD}$  is between ray  $\overrightarrow{AB}$  and ray  $\overrightarrow{AC}$ , then  $\overrightarrow{AD}$  intersects segment BC.
- 2. Do any three (3) of the following.
  - (a) Using any previous result, including the first part of the proposition, prove the second half of Proposition 3.3:
    - Given A\*B\*C and A\*C\*D, then A\*B\*D.
  - (b) Recall that a well-formed-statement (wfs) is **independent** of an axiomatic system if neither that statement nor its negation can be deduced from the axioms. Prove the following (wfs) is independent of the axioms of incidence geometry.
    - "For any two lines l and m there exists a one-to-one correspondence between the set of points incident with line l and the set of points incident with line m."
  - (c) Using any result up to and including Proposition 3.19, prove Proposition 3.20.(Angle Subtraction)
    - Given ray  $\overrightarrow{BG}$  between ray  $\overrightarrow{BA}$  and ray  $\overrightarrow{BC}$ , ray  $\overrightarrow{EH}$  between ray  $\overrightarrow{ED}$  and ray  $\overrightarrow{EF}$ ,  $\triangleleft CBG \cong \triangleleft FEH$ , and  $\triangleleft ABC \cong \triangleleft DEF$ . Then  $\triangleleft GBA \cong \triangleleft HED$ .
  - (d) Using any result up to and including part (a) of Proposition 3.9, prove the following. If D is a point interior to triangle  $\Delta ABC$ , then any ray emanating from D must intersect one of the sides of the triangle.
  - (e) Using any previous result, prove part (d) of Proposition 3.13. If AB < CD, and CD < EF, then AB < EF.